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Elastic-Plastic Connection Model Describing Dynamic Interactions of Component Connections

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Design evaluation of nuclear facilities would be facilitated by a numerical evaluation system that can evaluate both global and local behaviors under severe seismic loading. A critical part of such a system is the numerical model describing the dynamic physical interactions among component connections, called the elastic-plastic connection model. Here we propose such a model and use it to simulate dynamic interactions using real earthquake and plant data from the High Temperature Engineering Test Reactor (HTTR) at the Oarai Research and Development Center of the JAEA. We focus on joints connecting the component supports and the building walls, which generally involve fixed/pinned boundary conditions. Precision was increased by adjusting model parameters to fit experimental data. The results confirmed a reduction in the vibration response and a change in the natural frequencies of individual components under large virtual earthquake loading, which are considered to have resulted from dynamic interactions between the joints connecting the component supports and the building walls.

KEYWORDS: *elastic-plastic connection model, dynamic interaction, earthquake response, plant simulation*

I. Introduction

Public concern for earthquake safety and inspection of nuclear plants is increasing in light of recent revelations that, for example, the acceleration responses of a certain nuclear plant exceeded the design values during an earthquake. This is, indeed, a cause for worry and must be quickly addressed by evaluating the earthquake resistance of extant nuclear plants and proving sufficient factor of safety in structural strength. The 2004 White Paper on Nuclear Safety commissioned by the Nuclear Safety Commission of Japan¹⁾ states that the incidence of joint failure in plant components was comprise an equivalent of 65% of all failures. To address this, ideally, actual-scale experiments are necessary, which would allow precise determination of the properties of these joints. But the cost and time required makes this impractical. A conventional numerical simulation often requires the assumption of simple analysis conditions to reduce computational complexity when attempting to model the whole structure.²⁻⁴⁾ What is particularly needed is a model that can be used to determine the possibility of joint damage in mechanical and structural components under unusually large earthquake loads.

The objective of this research is to develop a numerical evaluation system that can evaluate both global and local behaviors of facilities under severe seismic loading. One important step toward realizing this objective is the development of a numerical model describing the dynamic interactions of component connections, called the elas-

tic-plastic connection model. We focus on the joints connecting the component supports and the building walls, which generally involve fixed/pinned boundary conditions. By introducing this elastic-plastic connection model into a large-scale elastic structural model,⁵⁾ it becomes possible to analyze the gestalt structural response, including all the local elastic-plastic behaviors of structures at the connections. In this manner, it becomes possible to evaluate both global and local behaviors of the structure.

First, to understanding of the mechanical behavior of the joints and validate the proposed elastic-plastic connection model, we conducted a hybrid experiment, which involved both an actual experimental load test and numerical simulation. This allowed investigation of the real seismic performance under large deformation and/or near the point of structural collapse under strong ground motion. This technique is effective for large-scale facilities, which cannot be tested in actual size. The experimental results revealed the characteristic dynamic behavior of the joints and allowed validation of the model by comparison with calculated predictions.

Furthermore, we applied the proposed elastic-plastic connection model to modeling joints in the High Temperature Engineering Test Reactor (HTTR) of the Japan Atomic Energy Agency (JAEA) as an example of a real-world application. We identified the effectiveness of the simulation by comparing the numerical results with the earthquake response observation records of HTTR at the elastic level and also inspected the influence of the elastic-plastic behavior at the connections on gestalt behavior under large simulated

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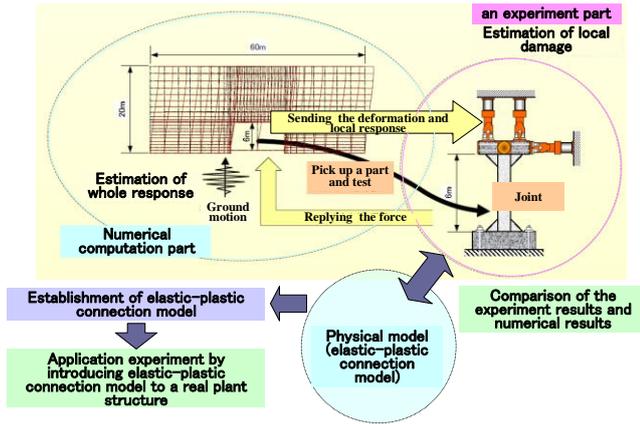


Fig. 1 Overview of the study

earthquake loads sufficient to damage some joints. The overview of the study is shown in Fig. 1.

II. Elastic-Plastic Connection Model

Here, the interaction between joints (including the embedded fastener) connecting component supports and the building walls (Fig. 2) was modeled using the proposed elastic-plastic connection model. The supports and the building transmit forces through the embedded fastener (Fig. 3). Note that during the conventional design process, cyclic loading is not considered for embedded fasteners. Rather, only simple vertical tension force, horizontal shear force, and combinations of the two are considered.⁶⁾ The proposed elastic-plastic connection model (Fig. 4), however, allows for the random cyclic loads seen during earthquakes. The conventional model covers a part of a beam element,^{7,8)} but we changed the specifications to be able to insert it over a part of a finite solid element and developed. In addition, the Ramberg-Osgood model⁹⁾ was introduced to model the elastic-plastic hysteresis and sliding at metal joints seen in the experiments (Fig. 5). Furthermore, though the conventional model was applicable to only a part of the structural member, the proposed model was developed to be applicable to both a part of the member and boundary interfaces. A benchmark test was performed by using the conventional model and the proposed model, as shown in Fig. 6. A vertical sin wave was loaded at the top of the model. The comparison between the results shows good agreement and it confirmed the validity of the assumed hysteresis model. In this way, the framework of elastic-plastic connection model was prepared.

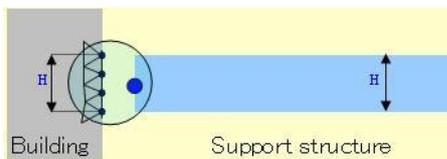


Fig. 2 Joint connecting the component supports and the building walls

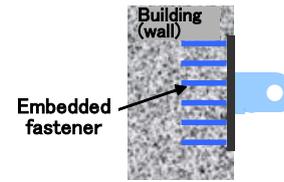


Fig. 3 Embedded fastener

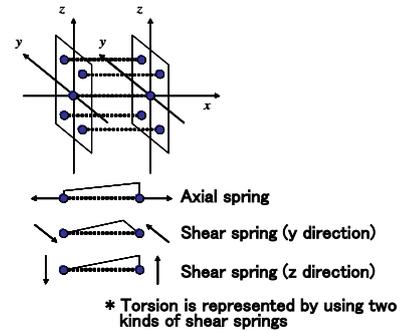


Fig. 4 Spring model of elastic-plastic connection

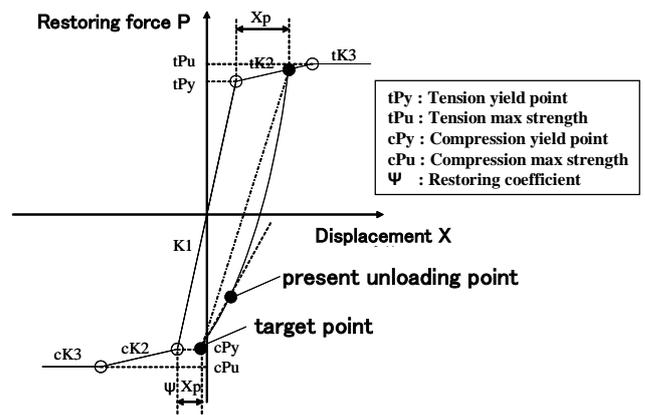


Fig. 5 Hysteresis characteristics of each spring (Ramberg-Osgood model)

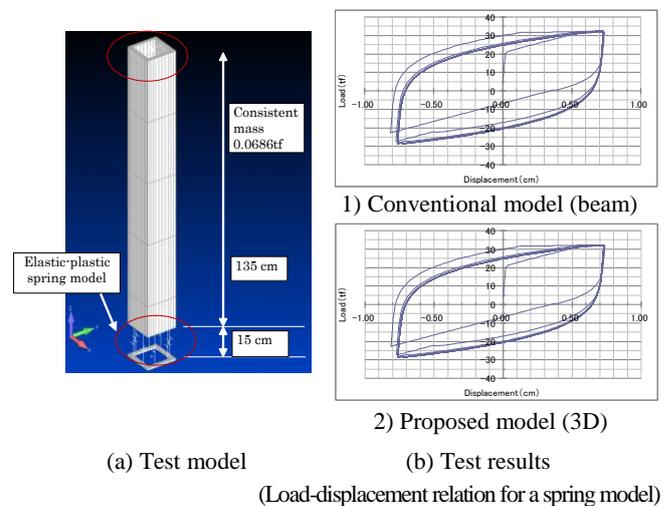


Fig. 6 Benchmark test

III. Hybrid Experiment

1. Methods Summary

When performing a loading experiment on the joints, it is critical to consider the interaction between the support structures and the building walls¹⁰⁻¹⁴⁾ and to clarify the mechanical characteristics of the joints under seismic load. However, when studying the seismic response of the piping system and heat exchanger, which are important facilities in a nuclear plant, large-scale experimental models are necessary, which entail considerable cost. Therefore, we resort to the hybrid experiment method, fusing numerical analysis and real experiment, as described in the Introduction. Briefly, actual experimental test specimens were created only for critical components, whereas the rest were simulated.

In this study, a hybrid seismic response experiment was performed for a total of five component support structures: four piping support structures and one equipment support structure. These specimen and all test cases are shown in **Table 1**. A photograph of the hybrid experiment setup for a piping support structure is shown in **Fig. 7**. Experimental models were fabricated for four kinds of framed restraints for piping support in actual size as shown in **Fig. 8** and an upper support structure for the intermediate heat exchanger (IHx) of HTTR on one-third scale as shown in **Fig. 9**. The main vibration modes of the whole experimental system, including the specimens, were determined in reference to the design information of HTTR. A real-time hybrid experiment system linked to the loading apparatus was performed by using fast dynamic hydraulic actuators and numerical simulation of the entire system on a high-speed computer.^{15,16)}

A narrow-band random wave covering 5–25 Hz, which included the main natural modes of the piping system and the equipment system, was used as the input wave for seismic loading. The amplitude of the input acceleration was increased in steps on the basis of observed specimen damage. More details on the experiment conditions may be found in Ref. 17).

2. Experimental Results

Examples of the load–displacement curves obtained from the hybrid seismic response experiment are shown in **Figs 10** and **11**. For the piping support, the dominant damage mode was via accumulated strain at the connections between the mechanical supports around the piping and the frame around the support. The load-displacement relations are shown in **Fig. 10** and the photos at the connections after the experiment are shown in **Fig. 12**. Note that previous studies, which used conventionally analysis, only considered simple forces and their combinations. Therefore, accurate experimental data on the behavior of the joints including the embedded fastener under large-scale random acceleration has not been previously reported. In this experiment for piping supports, we successfully obtained the data and observed some cracks on the surface of the RC structure around the connecting joints. On the other hand, a slipped load–displacement relation was observed at the low load level for the equipment support because of hinges in the joint as shown in **Fig. 11**.

Table 1 Specimen and experimental cases

Specimen Type	Structure type	Base type	Load type	Experimental Case	
SS	piping support	steel	Static cyclic	SS1	
			Seismic	SS2	
RC with embedded fastener		Fastener type 1	Static cyclic	CS1-1	
			Seismic	CS1-2	
		Fastener type 2	Static cyclic	CS1-3	
			Seismic	CS1-4	
CS2		shape 2	Fastener type 1	Seismic	CS2
CS3		shape 3	Fastener type 1	Seismic	CS3
IHx	equipment support	RC with embedded fastener	Static cyclic	IHX1	
			Seismic	IHX2	



Fig. 7 Hybrid experiment for a piping support

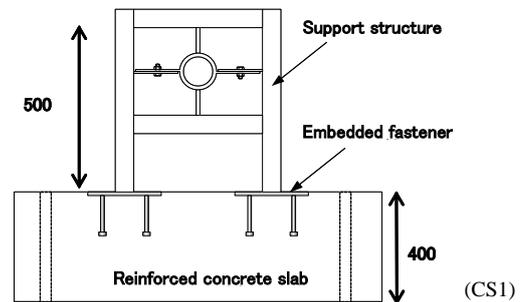


Fig. 8 One kind of piping support experimental specimens

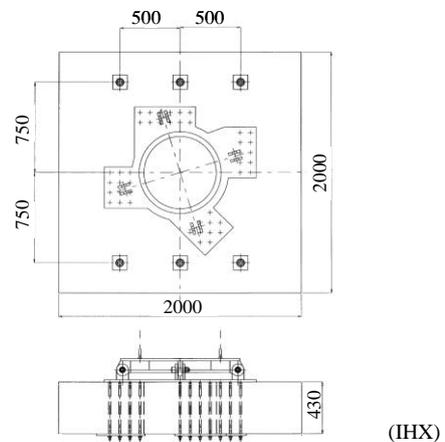


Fig. 9 Equipment support experimental specimen

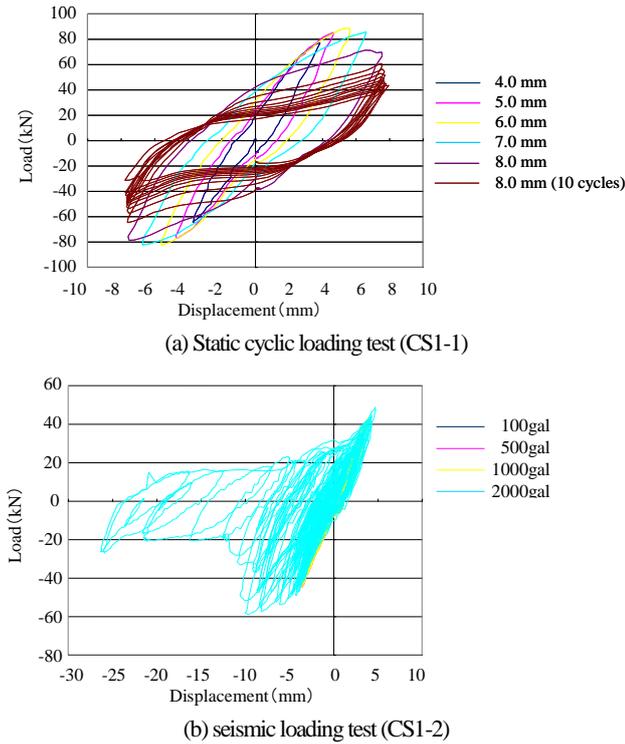


Fig. 10 Load-displacement relation for piping support

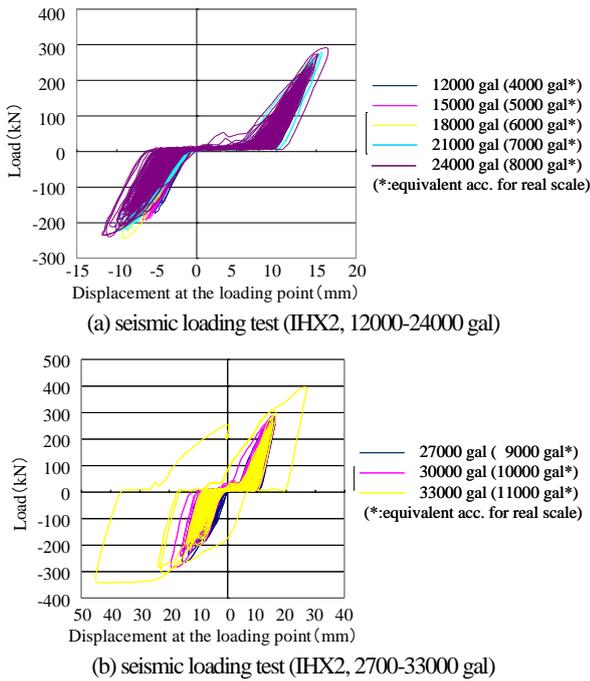


Fig. 11 Load-displacement relations for equipment support

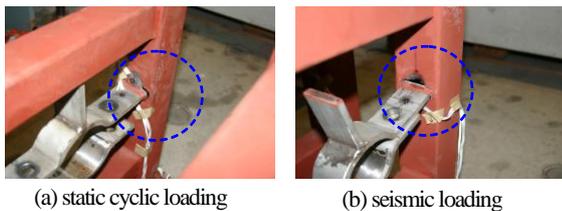


Fig. 12 Examples of experiment results. (a) deformed support pipe and (b) fatigue failure.

3. Comparison of Proposed Model and Experimental Results

To validate the proposed model, we substituted the experimental part of the hybrid experiment with a numerical model including the elastic-plastic connection model and compared the predictions with the previously obtained experiment results. The whole system including the piping support is shown in Fig. 13. The whole system including equipment support can be represented by using the structure system of IHX. These whole system were modeled as a one-degree-of-freedom model, as shown in Fig. 14. The each value of the natural frequency of the one-degree-of-freedom model represents the principal natural frequency of the corresponding whole system. Load-displacement relations of piping support and equipment support are shown in Figs. 15 and 16, respectively. It is found that the maximum load and displacement of both analytical results are well suited, whereas the stiffness, which is represented as a gradient of the graph, is a little difference that of the experimental results.

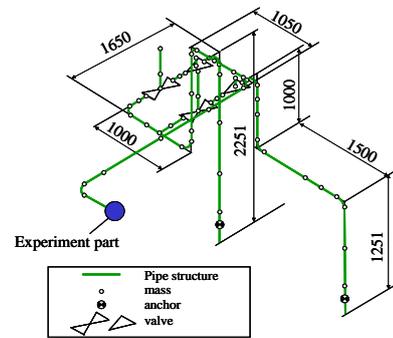


Fig. 13 Whole system including the piping support

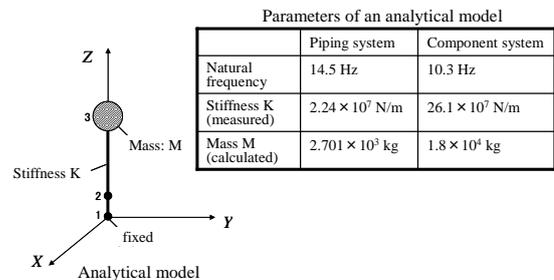


Fig. 14 Analytical model and the parameters

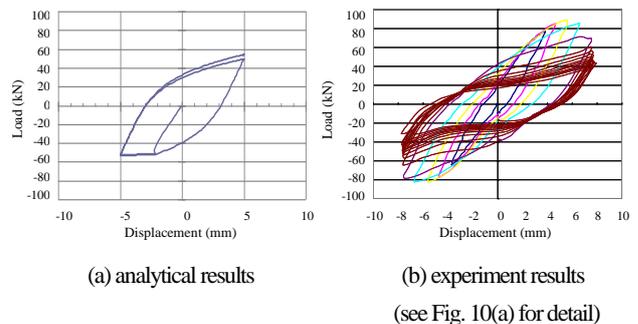


Fig. 15 Load-displacement relation (static cyclic loading of piping support) (see Fig. 10(a) for detail)

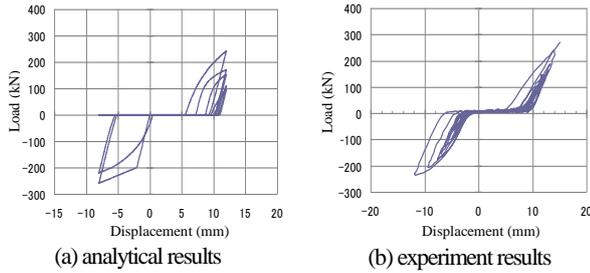


Fig. 16 Load-displacement relation (seismic loading of equipment support)

IV. Application to Real-Scale Plant Simulation

Seismic response analysis was performed for three kinds of real-scale plant systems, listed in **Table 2**. The primary cooling system, Model 1, is shown in **Fig. 17**. The joints were modeled by using three dimensional solid elements and springs, and the elastic-plastic connection models were inserted between the support structure and the building. Two cases of seismic response analysis were performed: case 1 using actual seismic observation records at the site, whose maximum accelerations at the base level of the building are 31 mm/sec^2 for horizontal direction and 15 mm/sec^2 for vertical direction, and case 2 using 200-times larger virtual seismic loads. It was confirmed that the predicted basic natural frequency in case 1 was almost equal to the observations in the elastic range (**Fig. 18**). In case 2, it was confirmed that the hysteresis characteristic of the elastic-plastic connection model could satisfy the given nonlinear rule even if the structure entered the strong nonlinearity area. Examples of the load-displacement relations are shown in **Fig. 19**. In addition, it was confirmed that the response of the component reduced when the joint was in the elastic-plastic area, and that the basic natural frequency changed. Examples of the time responses at the top of IHX are shown in **Fig. 20**. By analyzing the frequency characteristics of the time response, it was confirmed that the resonance frequency changed after joint damage shown in **Fig. 21**. This shows that the elastic-plastic connection model proposed in this research is applicable to a real scale plant simulation.

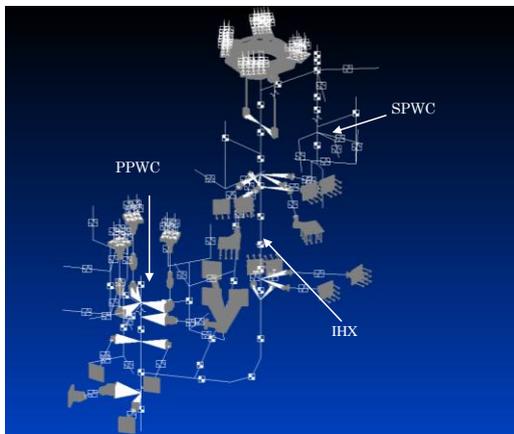


Fig. 17 Analytical model for whole numerical simulation including elastic-plastic connection model

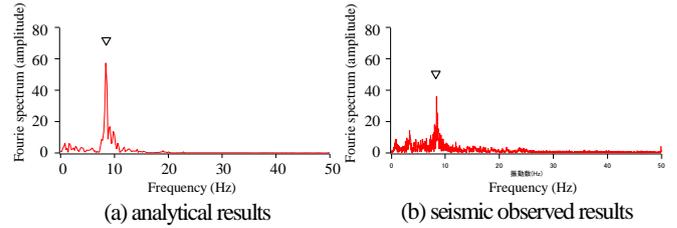
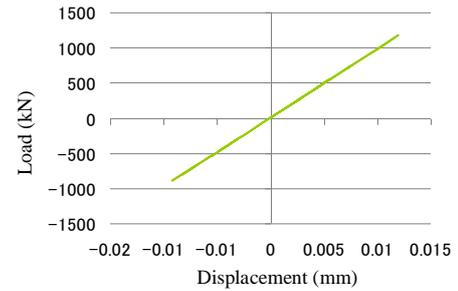
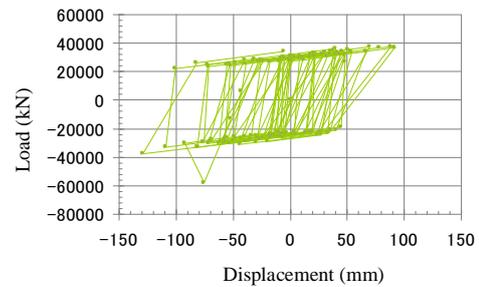


Fig. 18 Comparison of analytical results and seismic observations (Model 1, top of IHX)

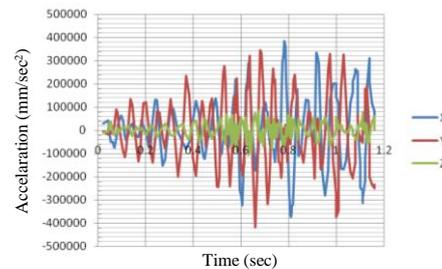


(a) without connection model

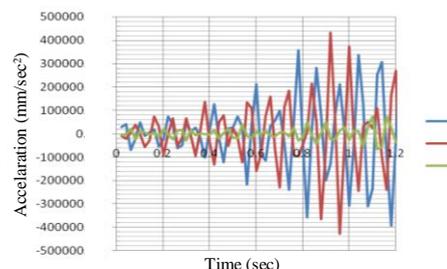


(b) with connection model

Fig. 19 Load-displacement relation at the joint (Model 1, top of IHX)



(a) without connection model

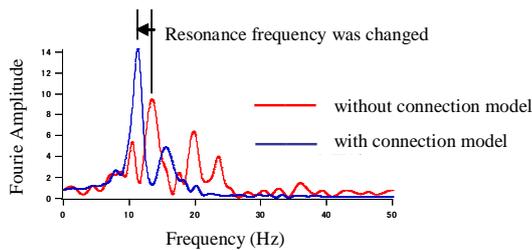


(b) with connection model

Fig. 20 Comparison of time response at the top of IHX (Model 1)

Table 2 Models for application experiment

	Object	Included equipment
Model 1	Primary cooling system	Intermediate heat exchanger (IHX), primary pressurized water cooler (PPWC), secondary pressurized water cooler (SPWC)
Model 2	Reactor pressure vessel	Reactor pressure vessel (RPV)
Model 3	Auxiliary cooling system	Auxiliary heat exchanger (AHX)

**Fig. 21** Comparison of the frequency response at the top of IHX (Model 1, x direction)

V. Conclusion

Our conclusions are as follows.

(1) Elastic-plastic connection model

The proposed elastic-plastic connection model for the joints connecting the component supports and the building walls successfully simulates the characteristic hysteresis properties seen in the experimental data, including the effect of the embedded fastener. The model enables structural analysis, permitting the damage of joints, which assumed as a fixed/pinned support in conventional analysis, was established.

(2) Hybrid experiment system

Hybrid experiments afford elastic-plastic hysteresis data and validate the proposed elastic-plastic connection model. In addition, valuable experimental data on the final damage mode for piping supports and equipment supports were obtained.

(3) Real scale plant simulation

A real scale plant simulation could be stably executed with the proposed elastic-plastic connection model, showing the effectiveness of the proposed model.

More detailed analysis will be necessary for complete evaluation of the earthquake-resistance of nuclear plants. Continued work along the present lines may allow detailed analysis of the seismic response of a complete nuclear plant.

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