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## ARTICLE

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# Atomistic Simulations of Stress Concentration and Dislocation Nucleation at Grain Boundaries

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Dislocation channeling observed in irradiated metals has been thought to be one of the key stress factors in irradiation assisted stress corrosion cracking since it is an evidence to suggest that the slip deformation is localized and that the strong misfit are generated at grain boundaries. In the present study, the stress concentration and defect nucleation of polycrystalline copper thin film is investigated by parallel molecular statics simulations. Uniaxial tensile deformation is applied to the two-dimensional polycrystalline model. As a result, it is found that the stress concentration is observed at triple point of grain junctions in the elastic and initial stage of plastic deformation. Then partial dislocations are first generated from the small angle grain boundaries. Twin deformations occur at triple points and grain boundaries which result in both another site of stress concentration around grain boundaries and local displacement relevant to the Burgers vector at grain boundary. One distinguishing characteristic of deformation mode of polycrystal is that the stress distribution strongly correlated with the presence of the partial dislocations and twin boundaries. Stress relaxation within each grain is preferentially brought about by the dislocation nucleation and twin deformation.

**KEYWORDS:** polycrystalline copper thin film, grain boundary, molecular statics, stress concentration, twin deformation

## I. Introduction

Irradiation assisted stress corrosion cracking (IASCC) is the urgent issue of the ageing management and maintenance in boiling water reactors.<sup>1-3)</sup> A large amount of experimental studies of IASCC have been so far reported. Recently, the dislocation channeling which is the unique deformation mode in irradiated materials is observed and that thought to be one of the dominant stress factors in IASCC.<sup>4)</sup> In this situation, glide dislocations interact with the grain boundaries which results in the stress concentration localized around grain boundary, and it is also worth considering that the local defect structures and local stress component change under deformation.

Grain boundary-dislocation process has been thought to be one of the most important factors in the crystalline materials which contribute significantly to plastic behavior as well as the dislocation-dislocation process. Though these two lattice defects have been efficiently introduced in material strengthening well-known as Hall-Petch relationship,<sup>5,6)</sup> they have the negative effects in the fracture behavior due to the stress concentration and segregation site at the boundary. Dislocations are successively piled up beside the grain boundary planes and they produce stress concentration which causes the secondary defect nucleation and cracking. Piled-up dislocations at grain boundaries, as well as the disappearance of dislocations from the interaction between the dislocations and the grain boundaries under indentation-induced stress, have been observed recently by in

situ nanoindentation with transmission electron microscopy.<sup>7)</sup>

Atomistic simulations have been used in a large number of studies of grain boundaries and dislocations. The equilibrium structures and corresponding fundamental grain boundary fault energies of various kinds of coincidence site lattice (CSL) grain boundaries were investigated.<sup>8)</sup> In focusing on the specific type of the CSL, the dislocation dissociation has been investigated by molecular dynamics simulation.<sup>9-11)</sup> The fundamental mechanisms of the interaction process between defect structures and individual crystal grain were comprehensively examined and showed the dissociation of the Burgers vector of glide dislocation in the interaction process. MD simulations have also been performed to capture the nanoscale plastic deformation of polycrystalline materials.<sup>12-14)</sup>

Focusing on the specific grain boundaries in our previous study, density functional theory calculations have been applied to evaluate the fault energies of the twin and several CSL grain boundaries, and molecular statics (MS) simulations are performed incipient plastic event on the twin and CSL grain boundaries.<sup>15)</sup> In the present study, we constructed two-dimensional thin film model and investigated the deformation characteristics of polycrystalline metal using MS simulations. The incipient yield event and local stress distribution under tensile deformation were discussed.

## II. Methods

### 1. Atomic Model

We constructed a two-dimensional polycrystalline copper

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using Voronoi polyhedra division. At first, the central points of Voronoi polyhedra were randomly scattered, where the minimum value of a distance between the points was corresponding to the diameters of the grains. In the present study, grain size was set to 20 nm. Then each grain region was determined by dividing between the scattered points. The single crystal oriented along the  $[1\bar{1}0]$ ,  $[1\bar{1}1]$  and  $[\bar{1}\bar{1}2]$  directions was prepared and embedded in the polyhedral region. Each crystal was rotated in the  $[\bar{1}\bar{1}2]$  axis at an arbitrary angle, where slip deformation is restricted to a single slip system, that is dislocations are activated on the same system in the plastic deformation of each grain. Atoms overlapping around the boundary are removed and the minimum distance between atoms is 70 percent of the nearest neighbor distance of perfect crystal. The atomic model of polycrystalline thin film is shown in **Fig. 1**. Here it has dimensions of  $150 \times 150 \times 1.33 \text{ nm}^3$  including thirty-seven grains. A stable configuration was obtained by finite temperature molecular dynamics and molecular statics with conjugate gradient (CG) energy minimization. Here, a parallel computing technique was employed in the present calculation.

## 2. Analysis Method

The fully-relaxed configuration of polycrystalline model was obtained by the CG method when the energy norm of all the atoms converged at 0.02 eV/Å, where the periodic boundary conditions were applied to all direction. The embedded atom method (EAM) type interatomic potential proposed by Mishin *et al.*<sup>16</sup> was employed. The validity of the fault energies and confirmations of specific grain boundaries evaluated using empirical potential has been investigated by comparing DFT calculations and it has been confirmed that the fundamental properties of grain boundaries in copper were reproduced correctly.<sup>15</sup>

Deformation analysis was performed by applying small increment of tensile strain in  $x$  direction, that is equal to 0.2% as shown in Fig. 1. Tensile stress  $\sigma_{xx}$  can be evaluated

after fully-relaxed configuration, where all stress components except for thickness direction were converged by controlling cell matrix. Similar analysis was performed for the single crystal with the same size which has dimensions of  $[\bar{1}\bar{1}0]$ ,  $[1\bar{1}1]$  and  $[\bar{1}\bar{1}2]$ . Atomic stresses of all atoms based on the Virial theorem were calculated in order to evaluate the local stress condition. The formulation of atomic stress in using EAM potential is expressed by following equation:

$$\sigma_{ij}^\alpha = \frac{1}{\Omega^\alpha} \sum_{\beta=1, \alpha \neq \beta}^N \left\{ \frac{1}{2} \phi'(r^{\alpha\beta}) + F'(\rho^\alpha) \tilde{\rho}'(r^{\alpha\beta}) \right\} \frac{r_i^{\alpha\beta} r_j^{\alpha\beta}}{r^{\alpha\beta}}, \quad (1)$$

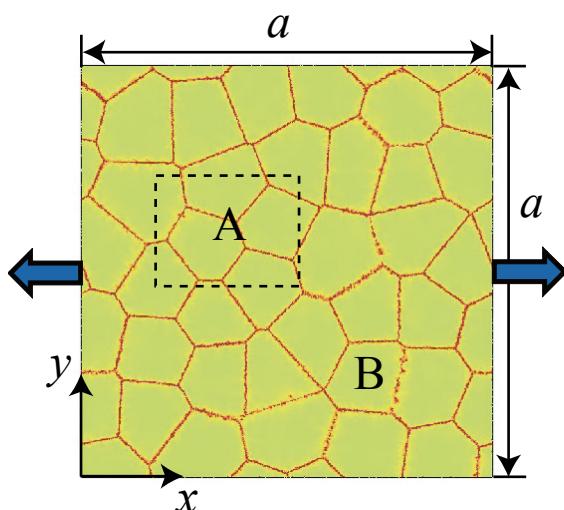
where  $\Omega^\alpha$  is the volume of atom  $\alpha$  and  $r^{\alpha\beta}$  is the distance between atom  $\alpha$  and atom  $\beta$ . The functions  $\phi$ ,  $F$  and  $\rho$  are the conventional forms of EAM potential corresponding to the pair potential term, the embedded function and the electron density function, respectively. The stress component of the whole system which is defined as the differentiation of the stored energy is obtained by averaging the atomic stress of all atoms as follows:

$$\sigma_{ij} = \frac{1}{V} \left( \frac{\partial E_{tot}}{\partial \varepsilon_{ij}} \right) = \frac{1}{N} \sum_{\alpha=1}^N \sigma_{ij}^\alpha, \quad (2)$$

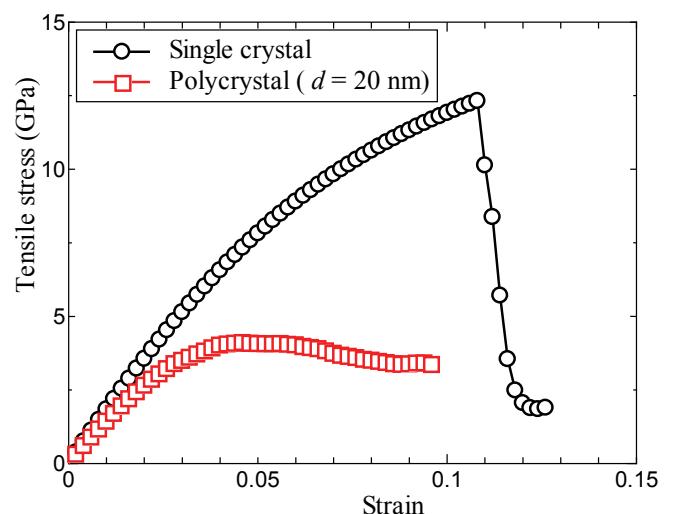
where  $V$  is the volume of the simulation box and  $N$  is the total number of atoms. Thus, the local stress in the vicinity of grain boundary and the stress of the system was evaluated efficiently.

## III. Results and Discussion

The relationships between tensile stress and strain of polycrystalline and single crystalline thin film are shown in **Fig. 2**. The yield stresses were found to be 4.09 and 12.3 GPa in polycrystal and single crystal, respectively. It is noted that higher tensile strength of single crystal is achieved only in the case that preexisting dislocation does not exist in the model. It is found that the presence of grain boundaries



**Fig. 1** Atomic model of polycrystalline copper thin film. Uniaxial tensile strain is applied along the  $x$  direction.



**Fig. 2** Relationship between tensile stress and strain of single crystal and polycrystalline copper

lead to a significant decrease in yield stress since the grain boundaries act as the sources of initial yield process such as dislocation nucleation. On the other hand, the amount of decrease in tensile stress after the yield point is smaller than that of single crystal.

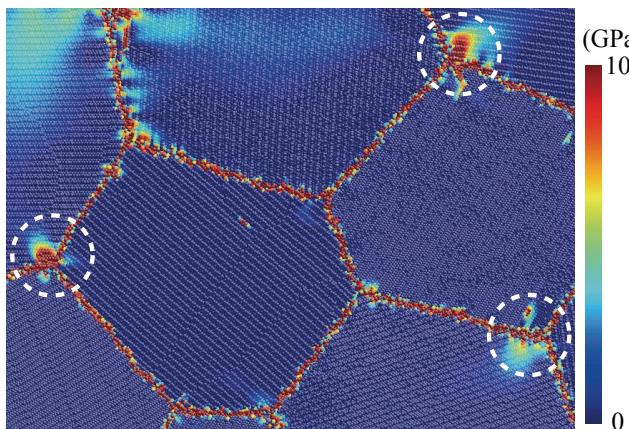
In elastic deformation region of polycrystal, stress is concentrated at the grain boundary triple junction. Focusing on the specific area A of Fig. 1, the distribution of Von Mises equivalent stress is shown in **Fig. 3**, where atomic configuration at  $\varepsilon = 0.02$  is depicted. It is confirmed that stress concentrations occur at several triple junctions enclosed by a white dash line. Therefore the triple junction would be an origin of the stress concentration which results in the early-stage yield event.

Except for the activation of preexisting dislocation, the initial plastic deformation polycrystalline model occurs around the small-angle grain boundaries. The structural changes of the early stage of plastic deformation are shown in **Fig. 4**. The area including Grain B is extracted from Fig. 1, where Grain B has a small-angle grain boundary in the right side. In Fig. 4 each atom is visualized by centro-symmetry parameter (CSP).<sup>17,18)</sup> The CSP is a structure-dependent scalar parameter defined as following equation:

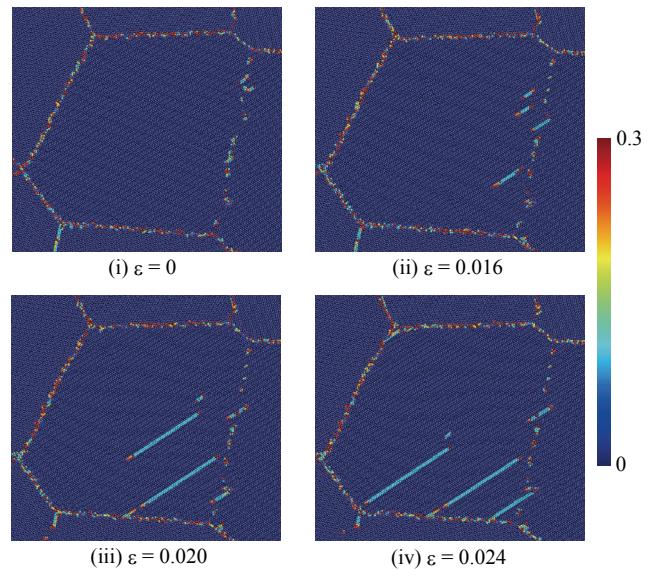
$$c_i = \sum_{i=1}^6 |\mathbf{r}_i + \mathbf{r}_{i+6}|^2 \quad (3)$$

where  $\mathbf{r}_i$  is the vector of the nearest neighbor atoms and the suffix  $i$  and  $i+6$  are a combination which is chosen according to the minimum square value. The value is normalized by the sum of the vectors.<sup>18)</sup> It is found that the early-stage plastic deformation occurs as dislocation emission while a stress-strain curve of whole system shows elastic deformation. Grain boundary dislocations (GBD) which construct a small angle grain boundary are first emitted since the GBDs are not restrained around the grain boundary region. Then GBDs are absorbed by other grain boundaries. As a result, the slope of elastic deformation in a stress-strain curve in the case of polycrystal is smaller after the GBDs are activated.

To investigate the relationship between internal structure and stress state, defect structures and stress distribution of whole system are shown in **Fig. 5(a)** and (b), respectively,



**Fig. 3** Stress concentration around grain boundary triple junction

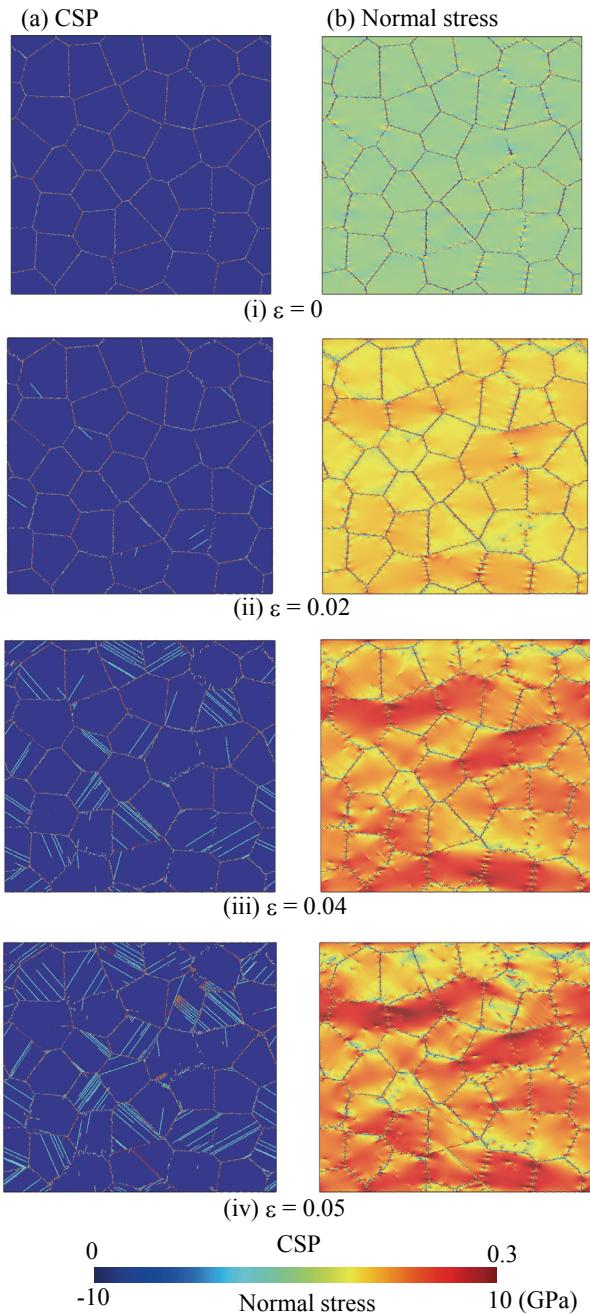


**Fig. 4** Snapshot of early-stage plastic deformation around small angle grain boundary under uniaxial tensile deformation

where defect structures including dislocations and twin boundaries are visualized by CSP and normal stress based on the atomic stress defined in Eq. (1) are shown. Each atom is color coded according to the stress component in the range  $-10 \leq \sigma_{11} \leq 10$  GPa. In the initial state, i.e. zero stress condition, there is no defect except for grain boundary region and atomic stresses with nonzero value are distributed around grain boundaries. Fig. 5(ii) is corresponding to the early stage elastic deformation, and it is confirmed that dislocations are activated from small angle grain boundaries and the triple point. Then a lot of dislocations emitted from other grain boundary regions are shown Fig. 5(iii) and (iv). In these stages, twin boundaries are nucleate between two edges of a grain. It should be considered that twin boundary have a greater tendency to be nucleated since deformation is constraint in the two-dimensional model with the present coordination system. In addition, it is found that the stress distribution strongly correlated with the presence of the partial dislocations and twin boundaries. That is a distinguishing characteristic of deformation mode of polycrystal. Stress relaxation within each grain is preferentially brought about by the dislocation nucleation and twin deformation.

#### IV. Conclusion

In conclusion, stress concentration and incipient yield mechanism of two-dimensional polycrystalline copper have been investigated by atomistic simulation. It is found that stress concentration is observed at the grain boundary triple junctions at the early stage elastic deformation and dislocations are first activated from small angle grain boundaries and triple junctions. A number of dislocations and twin boundaries are then nucleated from the other grain boundary regions. There is a strong correlation between stress distribution and local plastic deformation resulting from the stress relaxation caused by the defect nucleation.



**Fig. 5** Internal structures and stress state of deformed polycrystalline visualized by (a) CSP parameter and (b) normal stress in the tensile direction

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